## Impacts and Collisions

5. A smooth sphere A, of mass 3 kg , collides directly with another smooth sphere B, of mass 1 kg , on a smooth horizontal table.

Before impact A and B are moving in
 opposite directions with speeds of $5 \mathrm{~m} \mathrm{~s}^{-1}$ and $2 \mathrm{~m} \mathrm{~s}^{-1}$, respectively.
The coefficient of restitution for the collision is $\frac{1}{7}$.
Find (i) the speed of A and the speed of B after the collision
(ii) the loss in kinetic energy due to the collision
(iii) the magnitude of the impulse imparted to B due to the collision.
5. A smooth sphere A, of mass 2 kg , collides directly with another smooth sphere B, of mass 3 kg , on a smooth horizontal table.

A and B are moving in the same direction with speeds of $5 \mathrm{~ms}^{-1}$ and
 $4 \mathrm{~ms}^{-1}$ respectively.
The coefficient of restitution for the collision is $\frac{2}{3}$.
Find (i) the speed of A and the speed of B after the collision
(ii) the change in the kinetic energy of A due to the collision
(iii) the magnitude of the impulse imparted to A due to the collision.
5. A smooth sphere A, of mass 5 kg , collides directly with another smooth sphere $B$, of mass 2 kg , on a smooth horizontal table.

Before impact A and B are moving in
 opposite directions with speeds $3 \mathrm{~m} / \mathrm{s}$ and $5 \mathrm{~m} / \mathrm{s}$, respectively.
The coefficient of restitution for the collision is $\frac{3}{4}$.

Find (i) the speed of $A$ and the speed of $B$ after the collision
(ii) the loss in kinetic energy due to the collision
(iii) the magnitude of the impulse imparted to B due to the collision.

2008
5. A smooth sphere A, of mass 6 kg , collides directly with another smooth sphere B , of mass 5 kg , on a smooth horizontal table.

A and B are moving in opposite directions with speeds of $4 \mathrm{~m} / \mathrm{s}$ and
 $2 \mathrm{~m} / \mathrm{s}$ respectively.

The coefficient of restitution for the collision is $\frac{1}{10}$.

Find (i) the speed of A and the speed of B after the collision
(ii) the loss in kinetic energy due to the collision
(iii) the magnitude of the impulse imparted to A due to the collision.
5. A smooth sphere A, of mass 2 kg , collides directly with another smooth sphere $B$, of mass 3 kg , on a smooth horizontal table.
$A$ and $B$ are moving in the same direction with speeds of $5 \mathrm{~m} / \mathrm{s}$ and $2 \mathrm{~m} / \mathrm{s}$
 respectively.
The coefficient of restitution for the collision is $\frac{2}{3}$.
Find
(i) the speed of A and the speed of B after the collision
(ii) the loss in kinetic energy due to the collision
(iii) the magnitude of the impulse imparted to B due to the collision.
5. A smooth sphere A, of mass 2 kg , collides directly with another smooth sphere $B$, of mass 3 kg , on a smooth horizontal table.
$A$ and $B$ are moving in the same direction with speeds of $5 \mathrm{~m} / \mathrm{s}$ and $2 \mathrm{~m} / \mathrm{s}$
 respectively.
The coefficient of restitution for the collision is $\frac{2}{3}$.
Find
(i) the speed of A and the speed of B after the collision
(ii) the loss in kinetic energy due to the collision
(iii) the magnitude of the impulse imparted to B due to the collision.
5. A smooth sphere A, of mass 7 kg , collides directly with another smooth sphere $B$, of mass 3 kg , on a smooth horizontal table.
A and B are moving in opposite directions
 with speeds of $2 \mathrm{~m} / \mathrm{s}$ and $1 \mathrm{~m} / \mathrm{s}$ respectively.
The coefficient of restitution for the collision is $\frac{1}{3}$.
Find (i) the speed of A and the speed of B after the collision
(ii) the loss in kinetic energy due to the collision
(iii) the magnitude of the impulse imparted to A due to the collision.

2005
5. A smooth sphere $P$, of mass 2 kg , moving with a speed of $10 \mathrm{~m} / \mathrm{s}$ collides directly with a smooth sphere Q , of mass 3 kg , moving in the same direction with a speed of $5 \mathrm{~m} / \mathrm{s}$ on a smooth
 horizontal table.

The coefficient of restitution for the collision is $e$.
After the collision, sphere Q continues to travel in the same direction but with a speed of $8 \mathrm{~m} / \mathrm{s}$.
(i) Find the speed of P after the collision.
(ii) Find the value of $e$.
(iii) Find the fraction of kinetic energy lost due to the collision.
(iv) Find the magnitude of the impulse imparted to each sphere.
5. (a) A smooth sphere P , of mass 5 kg , moving with a speed of $2 \mathrm{~m} / \mathrm{s}$ collides directly with a smooth sphere Q , of mass 3 kg , moving in the opposite direction with a speed of $u \mathrm{~m} / \mathrm{s}$ on a smooth horizontal table.
The coefficient of restitution for the collision is $\frac{1}{2}$.
As a result of the collision, sphere P is brought to rest.
(i) Find the value of $u$.
(ii) Find the speed of Q after the collision.
(b) A ball is dropped from rest from a height of 1.25 m onto a smooth horizontal table. The ball hits the table with a speed of $v \mathrm{~m} / \mathrm{s}$ and then rebounds to a height of $h$ metres above the table.
The coefficient of restitution between the ball and the table is 0.8 .
(i) Find the value of $v$.
(ii) Find the value of $h$.

2003
5. A smooth sphere $P$, of mass 2 kg , moving with a speed of $3 \mathrm{~m} / \mathrm{s}$ collides directly with a smooth sphere Q , of mass 3 kg , moving in the opposite direction with a
 speed of $1 \mathrm{~m} / \mathrm{s}$ on a smooth horizontal table.
The coefficient of restitution for the collision is $e$.
As a result of the collision, sphere P is brought to rest.
(i) Find the speed of Q after the collision.
(ii) Find the value of $e$.
(iii) Find the fraction of kinetic energy lost due to the collision.
5. A smooth sphere $P$, of mass 2 kg , moving with a speed of $6 \mathrm{~m} / \mathrm{s}$ collides directly with a smooth sphere Q , of mass 4 kg , moving in the same direction with a speed of $4 \mathrm{~m} / \mathrm{s}$ on a smooth horizontal table.
The coefficient of restitution for the collision is $\frac{1}{2}$.
(i) Find the speed of P and the speed of Q after the collision.
(ii) Find the loss in kinetic energy due to the collision.
5. A smooth sphere $P$, of mass 4 kg , moving with a speed of $2 \mathrm{~m} / \mathrm{s}$ collides directly with a smooth sphere Q , of mass 2 kg , travelling in the opposite direction with a speed of $2 \mathrm{~m} / \mathrm{s}$ on a smooth horizontal table. The coefficient of restitution for the
 collision is $\frac{1}{3}$.
Find the speed of P and the speed of Q after the collision.
As a result of this collision Q goes on to collide directly with a stationary smooth sphere R , of mass 4 kg . The collision between Q and R causes Q to come to rest.

Find the coefficient of restitution for the collision between Q and R .
5. Two smooth spheres $P$ and $Q$, of masses 4 kg and 2 kg respectively and travelling in opposite directions with speeds of $5 \mathrm{~m} / \mathrm{s}$ and $4 \mathrm{~m} / \mathrm{s}$ respectively, collide directly on a smooth horizontal table.
The coefficient of restitution between the spheres
 is $e$.
As a result of the collision P continues to move in the same direction with a speed of $e \mathrm{~m} / \mathrm{s}$.
(i) Find the value of $e$.
(ii) Find the loss in kinetic energy due to the collision.

## ANSWERS

## 2011

(i) $\mathrm{v}_{1}=3 \mathrm{~m} \mathrm{~s}^{-1}$ and $\mathrm{v}_{2}=4 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) KE lost $=18 \mathrm{~J}$
(iii)Impulse $=6 \mathrm{~N} \mathrm{~s}$ or $6 \mathrm{kgms}^{-1}$

## 2010

(iv) $\mathrm{v}_{1}=4 \mathrm{~m} \mathrm{~s}^{-1}$ and $\mathrm{v}_{2}=14 / 3 \mathrm{~m} \mathrm{~s}^{-1}$
(v) Change in KE of $\mathrm{A}=9 \mathrm{~J}$
(vi) Impulse $=2 \mathrm{~N} \mathrm{~s}$

## 2009

(i) $\mathrm{v}_{1}=-1 \mathrm{~m} \mathrm{~s}^{-1}, \mathrm{v}_{2}=5 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) KE lost $=20 \mathrm{~J}$
(iii)Impulse $=20 \mathrm{~N} \mathrm{~s}$

## 2008

(i) $\mathrm{v}_{1}=1 \mathrm{~m} \mathrm{~s}^{-1}, \mathrm{v}_{2}=1.6 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) KE lost $=48.6 \mathrm{~J}$
(iii)Impulse $=18 \mathrm{Ns}$

## 2007

(i) $\mathrm{v}_{1}=2 \mathrm{~m} \mathrm{~s}^{-1}, \mathrm{v}_{2}=4 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) KE lost $=3 \mathrm{~J}$
(iii)Impulse $=6 \mathrm{Ns}$

## 2006

(i) $\mathrm{v}_{1}=0.8 \mathrm{~m} \mathrm{~s}^{-1}, \mathrm{v}_{2}=1.8 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) KE lost $=8.4 \mathrm{~J}$
(iii)Impulse $=8.4 \mathrm{~N} \mathrm{~s}$

2005
(i) $\mathrm{v}_{1}=5.5 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) $\mathrm{e}=0.5$
(iii)Fraction of KE lost $=9 / 110 \%$
(iv)Impulse $=9 \mathrm{~N} \mathrm{~s}$

2004 (a)
(i) $\mathrm{u}=14 / 9 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) $\mathrm{v}_{2}=16 / 9 \mathrm{~m} \mathrm{~s}^{-1}$

2004 (b)
$\mathrm{v}=5 \mathrm{~m} \mathrm{~s}^{-1}$
$\mathrm{h}=0.8 \mathrm{~m}$

## 2003

(i) $\mathrm{v}_{2}=1 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) $\mathrm{e}=0.25$
(iii)Fraction $=6 / 7 \%$

2002
(i) $\mathrm{v}_{1}=\mathrm{m} \mathrm{s}^{-1}, \mathrm{v}_{2}=5 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) KE lost $=2 \mathrm{~J}$

2001
(i) $\mathrm{v}_{1}=2 / 9 \mathrm{~m} \mathrm{~s}^{-1}, \mathrm{v}_{2}=14 / 9 \mathrm{~m} \mathrm{~s}^{-1}$
(ii) $\mathrm{e}=1 / 2$

2000 (a)
(i) $e=1 / 2$
(ii) loss in $\mathrm{KE}=40.5 \mathrm{~J}$

