Uniform Accelerated Linear Motion

1. The points P and Q lie on a straight level road.

A car passes P with a speed of 10 m s⁻¹ and accelerates uniformly for 6 seconds to a speed of 22 m s⁻¹.

The car then decelerates uniformly to a speed of 18 m s^{-1} and travels 80 m during this deceleration.

The car now maintains a constant speed of 18 m s⁻¹ for 3 seconds and then passes Q.

- Find (i) the acceleration
 - (ii) the deceleration
 - (iii) |PQ|, the distance from P to Q
 - (iv) the average speed of the car, correct to one decimal place, as it moves from P to Q.

- A car travels along a straight level road. It passes a point P at a speed of 12 ms⁻¹ and accelerates uniformly for 6 seconds to a speed of 30 ms⁻¹. It then travels at a constant speed of 30 ms⁻¹ for 15 seconds. Finally the car decelerates uniformly from 30 ms⁻¹ to rest at a point Q. The car travels 45 metres while decelerating.
 - Find (i) the acceleration
 - (ii) the deceleration
 - (iii) |PQ|, the distance from P to Q
 - (iv) the average speed of the car as it travels from P to Q.

2010

2011

1. 3 points *p*, *q* and *r* lie on a straight level road.

 $A \bigoplus_{p \neq q} P$

Two cars, A and B, are moving towards each other on the road.

Car A passes *p* with speed 3 m/s and uniform acceleration of 2 m/s² and at the same instant car B passes *r* with speed 5 m/s and uniform acceleration of 4 m/s².

A and B pass each other at q seven seconds later.

Find (i) the speed of car A and the speed of car B at q.

(ii) |pq| and |rq|, the distances A and B have moved in these 7 s.

Car A stops accelerating at q and continues on to r at uniform speed.

(iii) Find, correct to one place of decimals, the total time for car A to travel from p to r.

2008

 Four points a, b, c and d lie on a straight level road. A car, travelling with uniform retardation, passes point a with a speed of 30 m/s and passes point b with a speed of 20 m/s. The distance from a to b is 100 m. The car comes to rest at d.

- Find (i) the uniform retardation of the car
 - (ii) the time taken to travel from *a* to *b*
 - (iii) the distance from b to d
 - (iv) the speed of the car at c, where c is the midpoint of [bd].

A car travels from p to q along a straight level road. It starts from rest at p and accelerates uniformly for 5 seconds to a speed of 15 m/s.

It then moves at a constant speed of 15 m/s for 20 seconds.

Finally the car decelerates uniformly from 15 m/s to rest at q in 3 seconds.

- Draw a speed-time graph of the motion of the car from p to q. (i)
- (ii) Find the uniform acceleration of the car.
- Find the uniform deceleration of the car. (iii)
- (iv) Find |pq|, the distance from p to q.

1.

Find the speed of the car when it is 13.5 metres from *p*. **(v)**

2006

1. A car travels along a straight level road. It passes a point p at a speed of 10 m/s and accelerates uniformly for 5 seconds to a speed of 30 m/s. It then moves at a constant speed of 30 m/s for 9 seconds. Finally the car decelerates uniformly from 30 m/s to rest at point q in 6 seconds. Find (i) the acceleration

- (ii) the deceleration
 - (iii) |pq|, the distance from p to q
 - the average speed of the car as it travels from p to q. (iv)

2005

- 1. A particle travels from p to q in a straight line. It starts from rest at p and accelerates uniformly to its maximum speed of 20 m/s in 10 seconds. The particle maintains this speed of 20 m/s for 15 seconds before decelerating uniformly to rest at q in a further 20 seconds.
 - (i) Draw a speed-time graph of the motion of the particle from p to q.
 - Find the uniform acceleration of the particle. (ii)
 - Find the uniform deceleration of the particle. (iii)
 - (iv) Find |pq|, the distance from p to q.
 - Find the average speed of the particle as it moves from p to q, giving your answer (v)

in the form $\frac{a}{b}$, where $a, b \in \mathbb{N}$.

- 1. Three points *a*, *b* and *c*, lie on a straight level road such that |ab| = |bc| = 100 m. A car, travelling with uniform retardation, passes point *a* with a speed of 20 m/s and passes point *b* with a speed of 15 m/s.
 - (i) Find the uniform retardation of the car.
 - (ii) Find the time it takes the car to travel from *a* to *b*, giving your answer as a fraction.
 - (iii) Find the speed of the car as it passes c, giving your answer in the form $p\sqrt{q}$, where $p, q \in \mathbb{N}$.
 - (iv) How much further, after passing *c*, will the car travel before coming to rest? Give your answer to the nearest metre.

2003

- 1. A car travels from p to q on a straight level road. It passes p with a speed of 4 m/s and accelerates uniformly to its maximum speed of 8 m/s in 4 seconds. The car maintains this speed of 8 m/s for 6 seconds before decelerating uniformly to rest at q. The car takes 12 seconds to travel from p to q.
 - (i) Draw a speed-time graph of the motion of the car from p to q.
 - (ii) Find the uniform acceleration of the car.
 - (iii) Find the uniform deceleration of the car.
 - (iv) Find |pq|, the distance from p to q.

Another car travels the same distance from p to q in the same time of 12 seconds. This car starts from rest at p and accelerates uniformly to its maximum speed of v m/s and then immediately decelerates uniformly to rest at q.

(v) Find v, the maximum speed of this car, giving your answer as a fraction.

1. A train stops at stations P and Q which are 2000 metres apart. The train accelerates uniformly from rest at P, reaching a speed of 20 m/s in 10 seconds. The train maintains this speed of 20 m/s before decelerating uniformly at 0.5 m/s², coming to rest at Q.

- (i) Find the acceleration of the train.
- (ii) Find the time for which the train is decelerating.
- (iii) Find the distance and the time for which the train is travelling at constant speed.
- (iv) Draw an accurate speed-time graph of the motion of the train from P to Q.

2001



- (i) Find the speed of each car when they meet.
- (ii) Find the distance each car has travelled during this 10 seconds.

Suppose now that the speed of car A when passing point p is u m/s instead of 2 m/s, while the speed of car B passing point q and the acceleration of each car remain unchanged. If the time taken for the two cars to meet in this case is 8 seconds, find the value of u.

2000

1. A car is travelling on a straight stretch of level road [pq]. The car passes the point p with a speed of 5 m/s and accelerates uniformly to its maximum speed of 20 m/s in a time of 6 seconds. The car continues with this maximum speed for 30 seconds before decelerating uniformly to rest at q in a further 4 seconds.

Draw a speed-time graph of the motion of the car from p to q.

Hence, or otherwise, find

- (i) the uniform acceleration of the car
- (ii) the uniform deceleration of the car
- (iii) |pq|, the distance from p to q.

Another car, with acceleration and deceleration the same as in (i) and (ii) above, starts from rest at p and accelerates uniformly to its maximum speed of 25 m/s. It continues with this maximum speed for a certain time and then decelerates uniformly to rest at q. How long does it take this car to go from p to q?

Answers

2011

(i) $a = 2 \text{ m s}^{-2}$ (ii) $a = -4/3 \text{ m s}^{-2}$ (iii) |PQ| = 210 m(iv)Average speed = 17.5 m s⁻¹

2010

(v) $a = 3 \text{ m s}^{-2}$ (vi) $a = -10 \text{ m s}^{-2}$ (vii) |PQ| = 621 m(viii) Average speed = 25.875 m s⁻¹

2009

(i) $V_A = 17 \text{ m s}^{-1}$, $V_B = 33 \text{ m s}^{-1}$ (ii) $S_A = 70 \text{ m}$, $S_B = 133 \text{ m}$ (iii) t = 14.8 s 2008 (i) Retardation = 2.5 m s⁻² (ii) t = 4 s (iii)s = 80 m (iv)v = 14.1 m s⁻¹

2007

(i) (ii) $a = 3 \text{ m s}^{-2}$ (iii) $a = -5 \text{ m s}^{-2}$ (iv) s = 360 m(v) $v = 9 \text{ m s}^{-1}$

2006

(i) Acceleration = 4 m s⁻² (ii) Deceleration = 5 m s⁻² (iii)Distance = 460 m (iv)Average speed = 23 m s⁻¹

2005

(i) (ii) $a = 2 \text{ m s}^{-2}$ (iii)Deceleration = 1 m s⁻² (iv)s = 600 m (v) average speed = 40/3 m s⁻¹

2004

(i) Retardation = - 0.875 m s⁻² (ii) t = 40/7 s (iii) v = $5\sqrt{2}$ m s⁻¹ (iv) s = 29 m

2003

(i) (ii) $a = 1 \text{ m s}^{-2}$ (iii) $a = -4 \text{ m s}^{-2}$ (iv)s = 80 m(v) $v = 40/3 \text{ m s}^{-1}$

2002

(i) $a = 2 \text{ m s}^{-2}$ (ii) t = 40 s(iii)t = 75 s

2001

(i) $V_A = 22 \text{ m s}^{-1}$ $V_B = 31 \text{ m s}^{-1}$ (ii) $S_A = 120 \text{ m}$ $S_B = 160 \text{ m}$ (iii) $u = 14 \text{ m s}^{-1}$

2000

(i) (ii) Acceleration = 2.5 m s^{-2} (iii)Deceleration = 5 m s^{-2} (iv)Distance = 715 m(v) time = 36.1 s